

## Geometric properties

$A = H \cdot B [m^2]$  Cross section area

$d_s [m]$  Layer thickness  
(typical 60-500  $\mu m$ )

$n = \frac{L}{d_s} [-]$  Number of layers

## Material Properties

$\rho = 7.8e3 \frac{kg}{m^3}$  Density

$E = 36e9 \frac{N}{m^2}$  Young's modulus

$\nu = 0.34$  Poisson ratio

$\xi = 0.1$  Damping constant  
(estimate)

$-271^\circ C < T < 150^\circ C$  Operating temperature

$\epsilon_{33} = 300 - 4000$  Dielectric constant  
(typical value = 1750)

$d_{33} = 4e - 10 \frac{m}{V}$  Charge constant

$HC = 350 \frac{J}{kg \cdot K}$  Spec. heat capacity

$TC = 1.1 \frac{W}{mK}$  Spec. thermal conductivity

$-20V < U < 120V$  Typical voltage

## Mechanics

$\Delta L_{max} = \frac{L}{1000}$  Maximum displacement

$C_{axial} = \frac{EA}{L}$  Axial stiffness

$D = 2\xi\sqrt{C_{axial}m}$  Damping

$f_0 = \frac{1}{2\pi}\sqrt{\frac{C_{axial}}{m}}$  Resonance frequency

$t_{min} = \frac{1}{3f_0}$  Minimum rise time

$\varphi = 2 \arctan\left(\frac{f}{f_0}\right)$  Phase lag

$F_{blocking} = \Delta L_{max} \cdot C_{axial}$  Blocking force

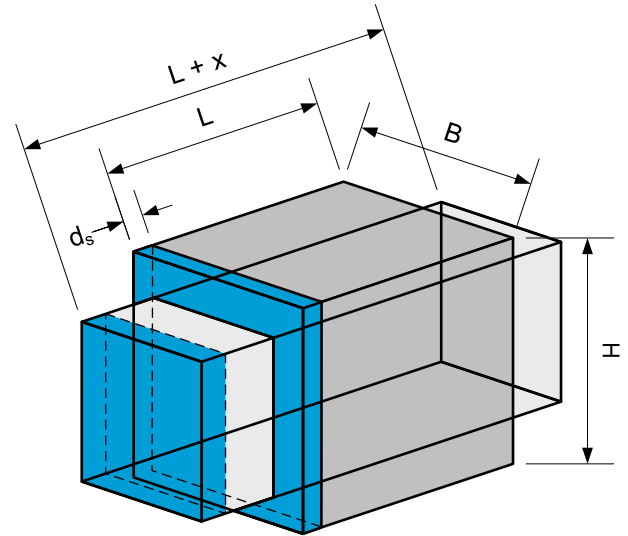
$\sigma_{dynamic} = 15 MPa$  Preload for dynamic use

$\sigma_{static} = 30 MPa$  Preload for static use

4 - 20 % Hysteresis

$\Delta x_{creep}(t) = x \cdot 0.01 \cdot \log\left(\frac{t}{0.1}\right)$  Creep @ t [s]

$F_{pre tension} = \frac{1}{2} F_{blocking}$  Pre tension force  
(matching push-pull force)



Geometric characteristics of a Piezo stack.

## Electronics

$x = d_{33} \cdot L \cdot \frac{U}{d_s}$  Displacement @ U [V]

$\epsilon_0 = 8.9e - 12 \frac{F}{m}$  Permittivity of free space

$C_S = n \cdot \epsilon_0 \cdot \epsilon_{33} \cdot \frac{A}{d_s}$  Small signal capacitance  
(typical for U < 100 V)

$C_L = 1.7 \cdot C_S$  Large signal capacitance  
(typical for U > 100 V)

$P = \frac{1}{2} \cdot f \cdot C \cdot U^2$  Average Polarization Power

$E = \frac{1}{2} \cdot C \cdot U^2$  Polarization energy

Not generic for all frequency ranges, just for indication:

$\tan \delta_U = 0.015 + 0.016 \sqrt{\frac{U}{[V]}}$  Loss factor @ U [V]

$\tan \delta_T = 0.28 + 0.17 \cdot \ln\left(\frac{T}{[K]}\right)$  Loss factor @ T [K]

$\tan \delta = \tan \delta_U + \tan \delta_T$  Loss factor  
 $P_{heat} = P \cdot \tan \delta$  Heat generation